

# **1 Analysis of thermospheric response to magnetospheric inputs**

Yue Deng, Astrid Maute, Arthur D. Richmond and Ray R. Roble

2 High Altitude Observatory, National Center for the Atmospheric Research,

3 Boulder Colorado, U.S.A.

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Yue Deng (e-mail: [ydeng@ucar.edu](mailto:ydeng@ucar.edu)), Astrid Maute (e-mail: [maute@ucar.edu](mailto:maute@ucar.edu)), Arthur D. Richmond  
(e-mail: [richmond@ucar.edu](mailto:richmond@ucar.edu)), Ray G. Roble (e-mail: [roble@ucar.edu](mailto:roble@ucar.edu)).

**Abstract.**

Coupling a new empirical model of the Poynting flux with the NCAR-TIEGCM, the influence of the high-latitude energy inputs and heating distributions on the global thermosphere are investigated. First, in order to show the contribution of the electric field variability to the energy input and thermospheric temperature, model results are compared for simulations where Joule heating is calculated with the average electric field (called "simple Joule heating") and where Joule heating is adjusted according to the Poynting flux from the empirical model. In the northern (summer) hemisphere, the Poynting flux has a peak in the dayside cusp, which is missing in the altitude-integrated simple Joule heating. The hemispheric integral of the Poynting flux is approximately 30% larger than the integral of simple Joule heating, and the polar average (poleward of  $40^\circ$ ) temperature calculated with the Poynting flux increases by 85-95 K, which is more than 50% of the temperature increase caused by the polar energy inputs. Second, three different methods to distribute the Poynting flux in altitude are investigated. Different heating distributions cause a difference in the polar average of heating per unit mass as high as 40% at 160 km altitude. Consequently, the difference of the polar average temperature among these three cases is close to 30-50 K. These results suggest that not only the total amount of energy input, but the way to distribute the energy in altitude is significant to the impact of the magnetosphere on the thermosphere and ionosphere.

## 1. Introduction

26 Electric fields and currents associated with magnetosphere-ionosphere interactions, along  
27 with auroral particle precipitation, are important sources of thermospheric energy and momen-  
28 tum, affecting the global thermospheric temperature, density, composition, and winds [e.g.,  
29 *Volland, 1979; Fuller-Rowell and Rees, 1980, 1981; Roble et al. 1982; Fuller-Rowell et al.,*  
30 *1987,1997; Rees and Ruller-Rowell, 1989; Crowley et al., 1989; Mikkelsen and Larsen, 1991;*  
31 *Rees, 1995; Rishbeth and Müller-Wodarg, 1999; Immel et al., 2001*]. The effects are strongest  
32 during and following magnetic storms, but also influence the quiet thermosphere. To develop  
33 first-principle thermospheric models with forecast capabilities therefore requires accurate in-  
34 formation about the magnetospheric inputs. Although global general-circulation models are  
35 able to reproduce the general features of thermospheric responses to magnetospheric inputs, the  
36 quantitative application of these models for predictive purposes is limited by uncertainties in  
37 the intensities and distributions of the inputs. This limitation applies not only to thermospheric  
38 general circulation models (TGCMs) used for analyses of thermospheric variability, like the Na-  
39 tional Center for Atmospheric Research (NCAR) Thermosphere-Ionosphere-Electrodynamics  
40 General-Circulation Model (TIE-GCM) [*Roble et al., 1988; Richmond et al., 1992*], the Cou-  
41 pled Thermosphere-Ionosphere-Plasmasphere model (CTIP) [*Millward et al., 2001*] and Global  
42 Ionosphere-Thermosphere model (GITM) [*Ridley et al., 2006*], but also to climatological mod-  
43 els that include coupling to the lower atmosphere, like the NCAR Thermosphere-Ionosphere-  
44 Mesosphere-Electrodynamics General-Circulation Model [*Roble and Ridley, 1994*] and the  
45 NCAR Whole Atmosphere Community Climate Model (WACCM) [*Garcia et al., 2007*].

Joule heating per unit volume,  $q_J$ , can be calculated from the relation

$$\begin{aligned} q_J &= \sigma_P (\mathbf{E} + \mathbf{u}_n \times \mathbf{B})^2 \\ &= \rho \lambda_P (\mathbf{E} \times \mathbf{B} / B^2 - \mathbf{u}_{n\perp})^2 \end{aligned} \quad (1)$$

$$\lambda_P = \sigma_P B^2 / \rho \quad (2)$$

where  $\sigma_P$  is the Pedersen conductivity,  $\lambda_P$  is the Pedersen ion-drag coefficient,  $\mathbf{E}$  is the electric field,  $\mathbf{B}$  is the magnetic field,  $\mathbf{u}_n$  is the neutral wind velocity,  $\mathbf{u}_{n\perp}$  is its component perpendicular to  $\mathbf{B}$ , and  $\rho$  is the neutral density. The Joule heating rate is related to the total electromagnetic energy transfer rate to the thermosphere,  $\mathbf{J} \cdot \mathbf{E}$  (where  $\mathbf{J}$  is the electric current density), by

$$\mathbf{J} \cdot \mathbf{E} = q_J + \mathbf{u}_{n\perp} \cdot \mathbf{J} \times \mathbf{B} \quad (3)$$

[e.g., *Lu et al.*, 1995; *Thayer et al.*, 1995; *Fujii et al.*, 1999]. The last term in (3) represents the rate of work done by the Ampère force on the wind. For time scales longer than a minute or so, the electromagnetic energy transfer rate equals the convergence of the perturbation Poynting vector (or Poynting flux)  $\mathbf{S}$ :

$$\mathbf{J} \cdot \mathbf{E} = -\nabla \cdot \mathbf{S} \quad (4)$$

$$\mathbf{S} = \mathbf{E} \times \Delta \mathbf{B} / \mu_0 \quad (5)$$

46 where  $\Delta \mathbf{B}$  is the magnetic perturbation due to ionospheric and field-aligned currents and  $\mu_0$   
 47 is the permeability of free space. If (4) is integrated over the entire volume of ionospheric  
 48 regions where  $\mathbf{J}$  has a component parallel to  $\mathbf{E}$  (essentially those regions of significant Pedersen  
 49 conductivity), and if Gauss' theorem is applied, it is found that the integral of the downward  
 50 component of  $\mathbf{S}$  over the top of the ionosphere,  $S_{\text{down}}$ , equals the volume integral of  $\mathbf{J} \cdot \mathbf{E}$ , since  
 51 the integral of the upward component of  $\mathbf{S}$  over the bottom of the ionosphere vanishes. In fact,

52 it is often a good approximation to relate the *local* value of  $S_{\text{down}}$  at the top of the ionosphere to  
 53 the height integral of  $\mathbf{J} \cdot \mathbf{E}$  [e.g., *Kelley et al.*, 1991]. *Gary et al.* [1994, 1995] have summarized  
 54 observations of  $S_{\text{down}}$  from Dynamics Explorer-2 (DE-2) spacecraft data. *Lu et al.* [1995] and  
 55 *Thayer et al.* [1995], using TGCM simulations, have shown that the height integrals of  $\mathbf{J} \cdot \mathbf{E}$  and  
 56 of  $q_J$  tend to be comparable, although positive or negative differences on the order of 25% can  
 57 exist. When further integrated horizontally [*Lu et al.*, 1995], the two quantities were found to  
 58 have very similar values. That is, in an average sense the net amount of electromagnetic energy  
 59 transfer to the kinetic energy of the wind (the last term in (3)) is usually only a small fraction  
 60 of the Joule heating and the local value of  $S_{\text{down}}$  approximately equals to the height integral  
 61 of Joule heating. ( We should note that estimates by *Fujii et al.* [1999] from EISCAT radar  
 62 measurements found a considerable fraction of  $\mathbf{J} \cdot \mathbf{E}$  going into  $\mathbf{u}_n \cdot \mathbf{J} \times \mathbf{B}$  on the average.  
 63 However, the estimation of  $\mathbf{u}_n \cdot \mathbf{J} \times \mathbf{B}$  from radar data is sensitive to the assumed model of  
 64 ion-neutral collision frequency, and so this result should be treated with caution.)

Empirical models have been developed to characterize the auroral precipitation [e.g., *Hardy et al.*, 1987, 1991; *Fuller-Rowell and Evans*, 1987; *Sharber et al.*, 2000] and high-latitude electric potential [e.g., *Foster et al.*, 1986; *Ruohoniemi and Greenwald*, 1996; *Ridley et al.*, 2000; *Weimer*, 2001] under various geophysical conditions. These empirical models are often used to force TGCMs. However, the models of the electric potential represent only the statistical average of the vector field  $\mathbf{E}$ ,  $\langle \mathbf{E} \rangle$ . The difference between  $\mathbf{E}$  and  $\langle \mathbf{E} \rangle$ ,

$$\mathbf{E}' = \mathbf{E} - \langle \mathbf{E} \rangle \quad (6)$$

65 is not negligible. For the purposes of the present work, we call  $\mathbf{E}'$  the “residual electric field.”  
 66 *Codrescu et al.* [1995] pointed out that  $\mathbf{E}'$  might contribute significantly to the total ther-  
 67 mospheric Joule heating, because of the non-linear dependence of the heating on the electric

68 field. Indeed, *Codrescu et al.* [2000], *Crowley and Hackert* [2001], and *Matsuo et al.* [2003]  
69 showed that the mean square of  $\mathbf{E}'$ ,  $\langle \mathbf{E}'^2 \rangle$  can be comparable to or even larger than the square  
70 of the mean  $\mathbf{E}$ ,  $\langle \mathbf{E} \rangle^2$ . It is expected that  $\mathbf{E}'$  varies considerably more rapidly than  $\langle \mathbf{E} \rangle$ , and in  
71 a rather random fashion, so that it will tend to be uncorrelated with  $\mathbf{u}_n$ , and the Poynting flux  
72 associated with it will therefore tend to go nearly entirely into Joule heating. Some modeling  
73 studies [e.g., *Emery et al.*, 1999] have attempted to account for the additional heating by mul-  
74 tipling the calculated Joule heating by a substantial factor, sometimes as large as 2.5, in order  
75 to obtain thermospheric responses that are reasonably consistent with observations. Because of  
76 the importance of the residual electric field on Joule heating, there is a need to quantify the Joule  
77 heating associated with it in a way consistent with the empirical model of electric potential used  
78 as TGCM inputs. In this paper, the Joule heating is specified two ways: one way, either calcu-  
79 lated from the average electric field, or specified by the Poynting flux from an empirical model  
80 based on the Dynamics Explorer 2 (DE-2) satellite data. The difference between them indicates  
81 the contribution from the residual electric field.

82 Because the thermosphere and ionosphere do not necessary respond in a linear fashion to  
83 the high-latitude energy inputs, certain aspects of their response can be quite sensitive to the  
84 intensity and distribution of the inputs. For example, the boundary between midlatitude regions  
85 where the  $O/N_2$  densities are increased or decreased during a storm, which strongly influences  
86 the boundary between regions of positive and negative ionospheric storm effects, depends on  
87 the intensity of high-latitude heating, with consequent upwelling and equatorward transport of  
88 molecular-rich air [e.g., *Richmond and Lu*, 2000]. Another nonlinear effect we will discuss fur-  
89 ther in the next section concerns the thermospheric response to distribution of the Joule heating.  
90 Concentrated heating can lead to significantly greater net upwelling of molecular species than

91 the same amount of total heating spread over a larger area [Smith, 2000]. In this study, three  
92 different ways to distribute the Poynting flux in altitude are compared to emphasize the response  
93 of thermosphere to the distribution of energy inputs.

## 2. Model description and simulation conditions

### 2.1. Poynting flux empirical model

94 A comprehensive, mutually consistent set of models of high-latitude thermospheric forcing is  
95 developed by analyzing observations of electric and magnetic fields and ion drift velocities from  
96 the DE-2 spacecraft, and will be detailed in a separate publication. An empirical model of the  
97 downward Poynting flux  $S_{\text{down}}$  at the top of the thermosphere is developed using the combined  
98 ion-drift and magnetometer data. The observations are fitted, at each magnetic latitude, to  
99 analytical functions of magnetic local time (MLT), dipole tilt angle with respect to the plane  
100 normal to the Sun-Earth line, and strength and clock angle of the  $B_y$  and  $B_z$  components of the  
101 interplanetary magnetic field (IMF).

102 Empirical models of the electric potential and of the horizontal component of  $\Delta B$  above the  
103 ionosphere are constructed from the DE-2 RPA/IDM and MAGB data, and parameterized in  
104 terms of the same parameters as the model of  $S_{\text{down}}$ , in order to have a mutually consistent  
105 set of models. Weimer [2001] used the DE-2 VEFI electric-field data to construct an empirical  
106 model of high-latitude electric potential, representing large-scale electric fields. Matsuo *et al.*  
107 [2003] fitted the potential to the DE-2 RPA/IDM data, with results generally consistent with  
108 the Weimer model [Weimer 2005] except for larger potentials at equinox when the IMF  $B_z$  is  
109 negative.

## 2.2. TIEGCM

110 The thermosphere general circulation model (TGCM) [Dickinson *et al.*, 1981, 1984] is a  
111 global circulation model that was developed at the National Center for Atmospheric Research  
112 (NCAR) in the early 80's. It calculates the properties of the upper atmosphere, such as the  
113 temperature, composition and wind velocity. The Thermosphere Ionosphere-GCM (TIGCM)  
114 [Roble *et al.*, 1988] includes a self-consistent ionosphere, and Thermosphere Ionosphere  
115 Electrodynamic-GCM (TIEGCM) [Richmond *et al.*, 1992] is an extension of this model that  
116 incorporates electrodynamic processes. The TIEGCM simulates self-consistently the neutral  
117 winds, conductivities, electric fields and currents. The model also calculates the neutral gas  
118 temperature and mass mixing ratios of  $O_2$ ,  $N_2$ ,  $O$ ,  $N(^2D)$ ,  $N(^4S)$  and  $NO$ . It also solves the  
119 electron and ion temperatures and the number densities of  $O^+$ ,  $O_2^+$ ,  $NO^+$ ,  $N_2^+$  and  $N^+$ . The  
120 model has  $5^\circ$  longitude by  $5^\circ$  latitude by  $1/2$  scale height resolution. The vertical coordinate  
121 has 29 constant pressure levels from approximately 97 km to 500 km altitude. At the lower  
122 boundary (97 km), the model is forced by tidal perturbations. Below  $60^\circ$  magnitude latitude the  
123 electric field is calculated by solving the electrodynamic equations, and above  $60^\circ$  latitude an  
124 electric potential pattern is imposed to describe the electric field.

## 2.3. Simulation conditions

125 The high-latitude forcing in the TIEGCM can be specified in different ways, and so there  
126 will be different ways in which the empirical high latitude driver models can be used to help  
127 specify the forcing. One mode of TIEGCM forcing is to use empirical climatological models of  
128 the forcing, varying in time according to the variations of the geophysical parameters used as  
129 inputs to the empirical model (e.g., day of year, UT, and  $K_p$ ). In this paper, the newly developed

130 empirical models provide the required high-latitude forcing: electric potential and downward  
 131 Poynting flux at the top of thermosphere.

132 Four TIEGCM runs are compared, which are called the "simple Joule heating" case, the  
 133 "Poynting-Joule" case, the "Poynting-Pedersen" case and the "Poynting-Diff" case, respec-  
 134 tively. For all of the cases, IMF  $B_z = -10nT$ ,  $F_{10.7} = 150 \times 10^{-22}W/m^2/Hz$  and the hemi-  
 135 spheric power (HP) is 16 GW. The simulated day number is 181, when the northern hemisphere  
 136 is in the summer and the southern hemisphere is in the winter. The differences among these runs  
 137 are the energy inputs in the high latitudes and the way to distribute the energy inputs in altitude.  
 138 For the "simple Joule heating" case, the TIEGCM is driven by the average electric potential  
 139 pattern from the empirical model and the energy input is the simple Joule heating, which is cal-  
 140 culated with the average electric field ( $q_e = q_{simple} = \sigma_p(\langle \mathbf{E} \rangle + \mathbf{u}_n \times \mathbf{B})^2$ ). For the "Poynting-  
 141 Joule" case, the Poynting flux is assumed to be equal to the height-integrated Joule heating. The  
 142 Poynting flux is then distributed in altitude proportionally to the calculated simple Joule heating  
 143 ( $q_e = \frac{q_{simple}}{\int_h q_{simple} dh} S_{down}$ ), and used in place of the previously calculated simple Joule heating. For  
 144 the "Poynting-Pedersen" case, it is the same as the "Poynting-Joule" case except the Poynting  
 145 flux is distributed in altitude according the Pedersen conductivity ( $q_e = \frac{\sigma_p}{\int_h \sigma_p dh} S_{down}$ ). For the  
 146 "Poynting-Diff" case, the altitude integrated simple Joule heating and the Poynting flux from  
 147 the empirical model are compared. When the Poynting flux is larger than the altitude integrated  
 148 simple Joule heating, the difference between them is then distributed in altitude according the  
 149 Pedersen conductivity ( $q_e = q_{simple} + \frac{\sigma_p}{\int_h \sigma_p dh} (S_{down} - \int_h q_{simple} dh)$ ); otherwise, the simple Joule  
 150 heating is reduced by the ratio of the Poynting flux to the altitude integrated simple Joule heat-  
 151 ing ( $q_e = q_{simple} \frac{S_{down}}{\int_h q_{simple} dh}$ ), in order to avoid the possibility of large negative heating at certain  
 152 locations. The energy inputs and the distribution methods are summarized in the table 1.

153 Table 1 : Energy inputs and altitude distribution methods

Case	Simple JH	Poynting-Joule	Poynting-Pedersen	Poynting-Diff
Energy input	simple JH	Poynting	Poynting	Poynting
Alt-distribute	NA	simple JH	Pedersen conductivity	difference according Pedersen

### 3. Results

#### 3.1. Energy inputs specified by simple Joule heating and Poynting flux

154 In GCMs, simple Joule heating is internally computed according to the GCM's algorithms,  
 155 based on the smoothed electric field, neutral wind and conductivity. The empirical model of the  
 156 Poynting flux gives the magnitude of the Poynting flux, which is then assumed to be equal to  
 157 the height-integrated Joule heating. Figure 1 shows the net electromagnetic energy flux from  
 158 the magnetosphere into the thermosphere, with the altitude-integrated simple Joule heating on  
 159 the left side and the Poynting flux from the empirical model on the right side. It is clear that  
 160 they have different distributions as well as different magnitudes. In the northern (summer)  
 161 hemisphere, the altitude-integrated simple Joule heating maximizes on the dawn and dusk sides,  
 162 while the Poynting flux has an additional peak in the noon-time cusp region. In the southern  
 163 (winter) hemisphere, the altitude-integrated simple Joule heating has a larger maximum value  
 164 on the duskside, and the Poynting flux has a more even distribution between dawnside and  
 165 duskside. In addition, the summer-winter difference is larger in the Poynting flux than in the  
 166 altitude integrated simple Joule heating. The large maximum of the Poynting flux at local noon  
 167 in the northern (summer) hemisphere is seasonally dependent and reduced significantly in the  
 168 winter. The total energy input (288 GW + 236 GW) for the Poynting flux case is 30% larger  
 169 than the simple Joule heating case (207 GW + 190 GW). In the empirical model, the Poynting  
 170 flux is computed using point measurements of the electric field and magnetic field, not the  
 171 smoothed fields, and shows the total electromagnetic energy input from the magnetosphere. On

172 the other hand, the simple Joule heating is calculated using the average electric field, which does  
173 not include small-scale variations. Thus, this 30% difference indicates the contribution of the  
174 electric field and conductivity variability to the total energy input. In this paper, we concentrate  
175 on the electric field variation assuming that the contribution of the small-scale conductivity  
176 variation is negligible. Since the Poynting flux has a more apparent cusp region peak in the  
177 northern (summer) hemisphere than the southern (winter) hemisphere, the following discussion  
178 concentrates on the northern (summer) hemisphere.

179 the Poynting flux from the empirical model represents the energy flux at the top of ther-  
180 mosphere, which has a two dimensional distribution. In order to get a three dimensional profile  
181 of the energy inputs, it is necessary to distribute the Poynting flux in altitude. In the polar re-  
182 gion, the magnetic field is almost vertical and the magnetic field lines are equipotentials, and it  
183 is reasonable to assume that electric field and magnetic field change little with altitude. If the  
184 neutral wind is ignored, the altitude distribution of Joule heating only depends on the Pedersen  
185 conductivity, and distributing the Poynting flux in height according the Pedersen conductivity  
186 is very straightforward. After this expansion, the horizontal distribution of the heating per unit  
187 mass in the northern (summer) hemisphere at a particular altitude (400 km), shown in Figure 2,  
188 is similar to the distribution of the total energy flux at the top of thermosphere, shown in Fig-  
189 ure 1. However, since the Pedersen conductivity is not uniform in space, the two distributions  
190 are not identical. For example, in the northern (summer) hemisphere, where the Poynting flux  
191 on the dawnside has a comparable magnitude as on the duskside, as shown on the right of Fig-  
192 ure 1(A), the heating per unit mass on the duskside at 400 km altitude, shown in the middle of  
193 Figure 2, is much larger than that on the dawnside.

194 Figure 3 shows the vertical wind distributions for the simple Joule heating case, Poynting flux  
195 case and the difference between them. The maximum vertical velocity is close to 10 m/s, which  
196 is relatively small compared with the horizontal velocity. In general, the vertical wind is upward  
197 on the dayside and downward on the nightside. The maximum upward wind and the maximum  
198 downward wind are separated by the day-night terminator. The vertical wind difference, shown  
199 on the right of Figure 3, shows a strong correlation with the heating difference, shown on the  
200 right of Figure 2. For example, the duskside maximum in the heating difference corresponds  
201 to a maximum in the upward neutral velocity difference, while the dawnside minimum in the  
202 heating difference corresponds to the minimum in the vertical velocity difference. Due to the  
203 complexity of the advection, the response of the vertical neutral velocity to the energy input is  
204 not linear. For example, while the difference heating in the cusp is smaller than that at dusk,  
205 the cusp difference neutral wind actually is larger than that on the duskside. Also, the peak  
206 positions do not totally overlap. The region of negative heating difference extends to later local  
207 times than does the negative wind difference, which is shifted toward the nightside by several  
208 hours.

209 Figure 4 represents the thermosphere-ionosphere response in the northern (summer) hemi-  
210 sphere when the energy inputs are specified by the simple Joule heating and by the Poynting  
211 flux. As shown in Figure 4(A), the temperature distributions for the simple Joule heating and  
212 the Poynting flux cases have similar structures, with higher temperatures in the afternoon sector  
213 than in the morning sector below  $60^\circ$  latitude. The difference of Poynting flux case from the  
214 simple Joule heating case is in the right column, which shows the temperature increases in the  
215 whole polar region with a maximum of more than 100 K. There are three temperature difference  
216 peaks, in the late-morning sector, on the dusk side, and around midnight. Interestingly, the tem-

217 perature difference does not correspond to the heating difference very well. This is because the  
218 temperature is under the influence of several mechanisms, including adiabatic cooling, thermal  
219 conductivity and advection, as well as heating. While there is no positive heating difference  
220 in Figure 2 at midnight, there is a positive neutral temperature difference peak in Figure 4 (A)  
221 around midnight at  $60^\circ$  latitude. This neutral temperature increase is possibly correlated with  
222 the downward neutral wind difference, shown in Figure 3 (B), which results in an adiabatic  
223 heating. The increased temperature brings more  $N_2$  to high altitudes, and thus the  $O/N_2$  ratio  
224 difference exhibits a negative correlation with the temperature difference. As shown in Figure 4,  
225 on the duskside, where there is a peak in the temperature difference, the  $O/N_2$  ratio decreases  
226 by more than 0.7 (around 40%) and creates a small green negative region. At 400 km altitude,  
227 where diffusion is more important than chemical reactions to the electron density, a rough cor-  
228 relation between the differences of the  $O/N_2$  ratio and electron density can be seen in Figure 4.  
229 The electron density decreases in most places where the  $O/N_2$  ratio difference is negative. The  
230 distributions show that both the  $O/N_2$  ratio and the electron density decrease more on the dusk  
231 side than on the dawn side.

232 Figure 5 displays the altitude profiles of the polar average (poleward of  $40^\circ$  for the northern  
233 hemisphere and poleward of  $-40^\circ$  for the southern hemisphere) heating per unit mass. At  
234 most altitudes, the heating per unit mass in the Poynting flux case is larger than that in the  
235 simple Joule heating case. Also, the summer-winter difference is greater for the Poynting flux  
236 case (red lines) than the simple Joule heating case (black lines). Below 300 km altitude, the  
237 larger summer-winter difference in Poynting flux case is partially due to the 20% greater total  
238 energy input in the summer hemisphere. As a consequence of the hemispherically symmetric  
239 distributions of electric field and particle precipitation in the empirical models, there is almost

no summer-winter difference for the simple Joule heating at low altitudes. Above 300 km, interestingly, the heating per unit mass in the winter hemisphere (dot lines) is larger than that in the summer hemisphere (solid lines). The explanation is that in response to the seasonal neutral composition change, winter F-region electron densities and thus Pedersen conductivities are generally larger in winter than in summer.

The polar average neutral temperature for both the simple Joule heating and the Poynting flux cases are shown in Figure 6. Using the Poynting flux leads to an 85 K temperature increase in the southern (winter) and 95 K increase in the northern (summer) hemisphere, as compared with the simple Joule heating case. In order to show whether these 85-95 K temperature increases are significant or not, we made another run without Joule heating. As shown in Figure 6, compared with the simple Joule heating case (black lines), the temperature decreases by 160 K (125 K) in the southern (northern) hemisphere when there is no Joule heating (green lines). Therefore, those 85-95 K temperature increases are more than 50% of the temperature changes caused by the polar energy inputs.

### 3.2. Impact of the Poynting flux distribution

When the average electric field and residual electric field are described separately, the Joule heating can be written as:

$$q_J = \sigma_p (\langle \mathbf{E} \rangle + \mathbf{E}' + \mathbf{u}_n \times \mathbf{B})^2 \quad (7)$$

$$q_J = \sigma_p (\langle \mathbf{E} \rangle + \mathbf{u}_n \times \mathbf{B})^2 + 2\sigma_p \mathbf{E}' \cdot (\langle \mathbf{E} \rangle + \mathbf{u}_n \times \mathbf{B}) + \sigma_p \mathbf{E}'^2 \quad (8)$$

In the "Poynting-Pedersen" case, which is discussed in section 3.1, the Poynting flux is assumed to equal to the altitude integrated Joule heating and the energy inputs are distributed

258 proportionally to the Pedersen conductivity. The assumption in this method is that the average  
259 electric field ( $\langle \mathbf{E} \rangle$ ), electric field variation ( $\mathbf{E}'$ ) and neutral wind ( $\mathbf{u}_n$ ) change little in altitude.  
260 Therefore, the energy input is proportional to the Pedersen conductivity. Two other methods are  
261 also investigated in this study: one way is to distribute the Poynting flux in height proportionally  
262 to the simple Joule heating calculated with the average electric field ( $\sigma_p(\langle \mathbf{E} \rangle + \mathbf{u}_n \times \mathbf{B})^2$ ). This  
263 method, called "Poynting-Joule", assumes that  $\mathbf{E}' \propto (\langle \mathbf{E} \rangle + \mathbf{u}_n \times \mathbf{B})$ , which implies that the  
264 neutral winds respond to the change of ion drag force very quickly and totally follow the electric  
265 field variation. The other way, named "Poynting-Diff", is to distribute the difference between  
266 the Poynting flux and the altitude-integrated simple Joule heating in altitude according to the  
267 Pedersen conductivity in regions where the Poynting flux is larger than the altitude-integrated  
268 simple Joule heating. For places where the Poynting flux is smaller than the altitude-integrated  
269 simple Joule heating, the simple Joule heating is reduced by a certain ratio to make the altitude-  
270 integrated Joule heating equal to the Poynting flux. In this way, it is assumed that the neutral  
271 wind does not respond to the electric field variation at all and the residual electric field,  $\mathbf{E}'$ , is not  
272 correlated with the average electric field  $\langle \mathbf{E} \rangle$ . The second term in equation (8) vanishes (on the  
273 average), and the difference between the Poynting flux and the altitude-integrated simple Joule  
274 heating is the third term in equation (8). This difference is proportional to  $\sigma_p$ , since  $\mathbf{E}'$  changes  
275 little with altitude. From the assumptions of the three methods, it seems that the "Poynting-  
276 Diff" is the most reasonable way to distribute the Poynting flux, since the neutral wind is not  
277 constant in altitude, nor does it respond to the electric field variation very rapidly. But in order  
278 to the evaluate the different methods, they need to be compared with observations to test which  
279 way matches the known features of thermospheric variability best.

280 Figure 7 shows the heating per unit mass at 400 km altitude for the three different ways  
281 to distribute the Poynting flux in altitude. Interestingly, the three cases have different alti-  
282 tude distributions of heating, while they have exactly the same energy inputs at the top of  
283 thermosphere. While the "Poynting-Joule" case has a maximum value on the dawn side, the  
284 "Poynting-Pedersen" distribution has more significant maxima in the cusp region and on the  
285 dusk side, and the "Poynting-Diff" has a similar distribution as the "Poynting-Pedersen" case,  
286 except that the dawn cell is enhanced.

287 In order to investigate the impact of the energy distributions on the thermosphere, the dif-  
288 ference of each case from the background case (simple Joule heating) is shown in Figure 8,  
289 including the difference distributions of the heating per unit mass, vertical wind and tempera-  
290 ture with respect to the simple Joule heating case. The vertical wind difference shows a strong  
291 influence from the heating difference, and basically, where there is a positive (negative) heat-  
292 ing difference, there is an upward (downward) vertical wind. Because the heating difference is  
293 not the only forcing for the vertical wind difference, there are some other vertical wind differ-  
294 ence peaks without corresponding heating difference peaks, such as the upward wind difference  
295 close to 02 LT around  $60^\circ$  latitude in the "Poynting-Pedersen" case. Figure 8 (C) shows that  
296 the "Poynting-Joule" case has the smallest temperature variations and the "Poynting-Pedersen"  
297 case has the largest. There is a persistent temperature increase maximum around 9-13 LT in the  
298 morning sector below  $60^\circ$  latitude, which is possibly caused by the variation of horizontal and  
299 vertical convection. The position of the second temperature difference peak varies from case to  
300 case. The "Poynting-Joule" case maximizes in the early morning sector around  $60^\circ$  latitude, but  
301 the "Poynting-Pedersen" case has a maximum on the dusk side, which is related to the maxi-  
302 mum Poynting flux on the dusk side, as shown in Figure 8 (A). The "Poynting-Diff" case has a

303 similar distribution as the "Poynting-Pedersen" case, except that the magnitude is reduced. The  
304 distribution of the temperature difference does not correspond to the heating difference very  
305 well, which is due to the contribution of other mechanisms, such as adiabatic cooling, thermal  
306 conductivity and advection, as mentioned in the previous section.

307 As shown in Figure 9 (A), the polar average heating per unit mass in the northern (summer)  
308 hemisphere in the "Poynting-Joule" case (blue line) is smaller than in the "Poynting-Diff" case  
309 (green line) and "Poynting-Pedersen" case (red line) above 120 km altitude, while the total en-  
310 ergy inputs from magnetosphere are the same. At 160 km altitude, the "Poynting-Joule" is 40%  
311 smaller than "Poynting-Pedersen", which is caused by the differences in altitude distribution  
312 of energy associated primarily with wind effects. As shown in Figure 9 (B), more energy is  
313 distributed below 120 km altitude in the "Poynting-Joule" case than in the "Poynting-Pedersen"  
314 case, and the absolute value of the heating difference is larger below 120 km altitude than above  
315 120 km. However, due to the exponential decrease of mass density with height, the difference  
316 of heating per unit mass above 120 km is more significant. Figure 10 shows that all cases using  
317 the Poynting flux to specify the energy input have a consistent enhancement of the polar average  
318 neutral temperature compared with the simple Joule heating case, and the increased amplitude in  
319 the northern hemisphere varies from 40 to 95 K depending on the way to distribute the Poynting  
320 flux in altitude. This result indicates not only the total energy input, but also the distribution of  
321 energy can make some difference to the thermospheric response to the magnetospheric inputs.

#### 4. Conclusion and discussion

322 A new set of quantitative empirical models of the high-latitude forcing of the thermosphere,  
323 including electric potential and Poynting flux, are used with the NCAR-TIEGCM to investigate

324 the influence of the high-latitude forcing on the neutral temperature, composition and electron  
325 density.

326 First, the simple Joule heating calculated with the average electric field and the Poynting flux  
327 from the empirical model are compared to show the contribution of electric field variability to  
328 the Joule heating. The total energy of the Poynting flux is close to 30% larger than the inte-  
329 grated simple Joule heating. In the northern (summer) hemisphere, the Poynting flux has an  
330 apparent cusp peak, which is missing in the altitude-integrated simple Joule heating. Due to  
331 the non-uniform distribution of the conductivity, the distribution of heating per unit mass at 400  
332 km altitude is different from the distribution of total energy flux at the top of thermosphere.  
333 In general, the vertical wind difference between the Poynting flux case and the simple Joule  
334 heating case is upward (downward) where the heating per unit mass difference is positive (neg-  
335 ative). The neutral temperature in the Poynting flux case increases in the whole polar region  
336 compared with the simple Joule heating case and the increased magnitude can reach 100 K.  
337 The distribution of temperature difference does not correspond very well to the distribution of  
338 heating difference, because other mechanisms, such as adiabatic cooling, thermal conductivity  
339 and advection, are important to the temperature as well as the energy source. The decreased  
340  $O/N_2$  ratio shows an inverse relationship with the temperature change, and leads to an electron  
341 density reduction in almost the whole polar region. The polar average temperature increases by  
342 85-95 K, which is more than 50% of the temperature change caused by the polar energy inputs.

343 Secondly, the inter-comparison among three different methods to distribute the Poynting flux  
344 in altitude is conducted. The increase of the heating per unit mass, compared with the simple  
345 Joule heating case at 400 km altitude, has different distributions and magnitudes for the three  
346 cases. The resulting maximum increase of the temperature varies from 60 to 135 K. Due to

347 the differences in altitude distribution of heating, the polar average of the heating per unit mass  
348 for the "Poynting-Joule" case can be 40% smaller than the "Poynting-Pedersen" case around  
349 160 km altitude, while these two cases have the same amount of the total energy input from the  
350 magnetosphere. The corresponding difference of the polar average temperature between these  
351 two cases is close to 50 K in the northern hemisphere. This result suggests that not only the  
352 total amount of energy input, but the way to distribute the energy are important to the impact of  
353 magnetospheric forcing on the thermosphere and ionosphere.

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#### **References**

357 Codrescu, M.V., T.J. Fuller-Rowell, and J.C. Foster, On the importance of E-field variability  
358 for Joule heating in the high-latitude thermosphere, *Geophys. Res. Lett.*, 22, 2393-2396, 1995.

359 Codrescu, M.V., T.J. Fuller-Rowell, J.C. Foster, J.M. Holt, and S.J. Cariglia, Electric field  
360 variability associated with the Millstone Hill electric field model, *J. Geophys. Res.*, 105, 5265-  
361 5273, 2000.

362 Crowley, G., and C.L. Hackert, Quantification of high latitude electric field variability, *Geo-*  
363 *phys. Res. Lett.*, 28, 2783-2786, 2001.

364 Crowley, G., B. A. Emery, R. G. Roble, H. C. Carlson, Jr., and D. J. Knipp, Thermospheric  
365 dynamics during September 18-19, 1984, 1. Model simulations, *J. Geophys. Res.*, 94, 16,925-  
366 16,944, 1989.

367 Dickinson, R. E., E. C. Ridley, and R. G. Roble, A three-dimensional time-dependent general  
368 circulation model of the thermosphere, *J. Geophys. Res.*, *86*, 1499, 1981.

369 Dickinson, R. E., E. C. Ridley, and R. G. Roble, Thermospheric general circulation with  
370 coupled dynamics and composition, *J. Atmos. Solar-Terr. Phys.*, *41*, 205, 1984.

371 Emery, B.A., C. Lathuillere, P.G. Richards, R.G. Roble, M.J. Buonsanto, D.J. Knipp, P.  
372 Wilkinson, D.P. Sipler, and R. Niciejewski, Time dependent thermospheric neutral response  
373 to the 2-11 November 1993 storm period, *J. Atmos. Solar-Terr. Phys.*, *61*, 329-350, 1999.

374 Foster, J.C., J.M. Holt, R.G. Musgrove, and D.S. Evans, Ionospheric convection associated  
375 with discrete levels of particle precipitation, *Geophys. Res. Lett.*, *13*, 656-659, 1986.

376 Fujii, R., S. Nozawa, S.C. Buchert, and A. Brekke, Statistical characteristics of electromag-  
377 netic energy transfer between the magnetosphere, the ionosphere, and the thermosphere, *J. Geo-  
378 phys. Res.*, *104*, 2357-2365, 1999.

379 Fuller-Rowell, T., and Evans, D. S., Height-integrated Pedersen and Hall conductivity pat-  
380 terns inferred from the TIROS-NOAA satellite data, *J. Geophys. Res.*, *92*, 7606-7618, 1987.

381 Fuller-Rowell, T., and D. Rees, A three-dimensional time-dependent global model of the  
382 thermosphere, *J. Atmos. Sci.*, *37*, 2545-2567, 1980.

383 Fuller-Rowell, T.J., and D. Rees, A three-dimensional time-dependent simulation of the  
384 global dynamical response of the thermosphere to a geomagnetic substorm, *J. Atmos. Terr.  
385 Phys.*, *43*, 701-721, 1981.

386 Fuller-Rowell, T.J., S. Quegan, D. Rees, R.J. Moffett, and G.J. Bailey, Interactions be-  
387 tween neutral thermospheric composition and the polar ionosphere using a coupled ionosphere-  
388 thermosphere model, *J. Geophys. Res.*, *92*, 7744-7748, 1987.

389 Fuller-Rowell, T.J., M.V. Codrescu, B.G. Fejer, W. Borer, F. Marcos, and D.N. Anderson,  
390 Dynamics of the low-latitude thermosphere: quiet and disturbed conditions, *J. Atmos. Solar-*  
391 *Terr. Phys.*, 59, 1533-1540, 1997.

392 Gary, J. B., R. A. Heelis, W. B. Hanson, and J. A. Slavin, Field-aligned Poynting flux obser-  
393 vations in the high-latitude ionosphere, *J. Geophys. Res.*, 99, 11417-11427, 1994.

394 Gary, J.B., R.A. Heelis, and J.P. Thayer, Summary of field-aligned Poynting flux observations  
395 from DE2, *Geophys. Res. Lett.*, 22, 1861-1864, 1995.

396 Garcia, R. R., D. R. Marsh, D. E. Kinnison, B. A. Boville, and F. Sassi, Simulation of secular  
397 trends in the middle atmosphere, 1950-2003, *J. Geophys. Res.*, 112, 9301+, 2007.

398 Hardy, D.A., M.S. Gussenhoven, R. Raistrick, and W.J. McNeil, Statistical and functional  
399 representations of the pattern of auroral energy flux, number flux, and conductivity, *J. Geophys.*  
400 *Res.*, 92, 12,275-12,294, 1987.

401 Hardy, D.A., W. McNeil, M.S. Gussenhoven, and D. Brautigam, A statistical model of auroral  
402 ion precipitation, 2. Functional representation of the average pattern, *J. Geophys. Res.*, 96,  
403 5539-5547, 1991.

404 Immel, T.J., G. Crowley, J.D. Craven, and R.G. Roble, Dayside enhancements of ther-  
405 mospheric O/N<sub>2</sub> following magnetic storm onset, *J. Geophys. Res.*, 106, 15,471-15,488, 2001.

406 Kelley, M.C., D.J. Knudsen, and J.F. Vickrey, Poynting flux measurements on a satellite: a  
407 diagnostic tool for space research, *J. Geophys. Res.*, 96, 201-207, 1991.

408 Lu, G., A.D. Richmond, B.A. Emery, and R.G. Roble, Magnetosphere-ionosphere-  
409 thermosphere coupling: effect of neutral wind on energy transfer and field-aligned current, *J.*  
410 *Geophys. Res.*, 100, 19,643-19,659, 1995.

411 Matsuo, T., *Effects of high-latitude ionospheric electric field variability on the estimation of*  
412 *global thermospheric Joule heating*, Ph.D. thesis, State University of New York at Stony Brook,  
413 2003.

414 Matsuo, T., A.D. Richmond, and D.W. Nychka, Modes of high-latitude electric field variabil-  
415 ity derived from DE-2 measurements: Empirical Orthogonal Function (EOF) analysis, *Geophys.*  
416 *Res. Lett.*, 29(7), 1107, doi:10.1029/2001GL014077, 2002.

417 Matsuo, T., A. D. Richmond, and K. Hensel, High-latitude ionospheric electric field variabil-  
418 ity and electric potential derived from DE-2 plasma drift measurements: Dependence on IMF  
419 and dipole tilt, *J. Geophys. Res.*, 108(A1), 1005, doi:10.1029/2002JA009429, 2003.

420 Mikkelsen, I.S., and M.F. Larsen, A numerical modeling study of the interaction between  
421 the tides and the circulation forced by high-latitude plasma convection, *J. Geophys. Res.*, 96,  
422 1203-1213, 1991.

423 Millward, G.H., A.D. Aylward, I.C.F. Mueller-Wodarg, T.J. Fuller-Rowell, R.J. Moffett, and  
424 A.D. Richmond, An investigation into the influence of tidal forcing on F region equatorial ver-  
425 tical ion drift using a global ionosphere-thermosphere model with coupled electrodynamics, *J.*  
426 *Geophys. Res.*, 106, 24,733-24,744, 2001.

427 Rees, D., Observations and modelling of ionospheric and thermospheric disturbances during  
428 major geomagnetic storms: a review, *J. Atmos. Terr. Phys.*, 57, 1433-1457, 1995.

429 Rees, D., and T.J. Fuller-Rowell, The response of the thermosphere and ionosphere to mag-  
430 netospheric forcing, *Phil. Trans. Roy. Soc. London*, A328, 139-171, 1989.

431 Richmond, A.D., Assimilative mapping of ionospheric electrodynamics, *Adv. Space Res.*, 12,  
432 (6)59-(6)68, 1992.

433 Richmond, A.D., Ionospheric electrodynamics using Magnetic Apex Coordinates, *J. Geo-*  
434 *magn. Geoelectr.*, 47, 191-212, 1995.

435 Richmond, A.D., and G. Lu, Upper-atmospheric effects of magnetic storms: a brief tutorial,  
436 *J. Atmos. Solar-Terr. Phys.*, 62, 1115-1127, 2000.

437 Richmond, A.D., and J.P. Thayer, Ionospheric electrodynamics: a tutorial, in *Magnetospheric*  
438 *Current Systems*, edited by R.L. Lysak, M. Hesse, R. Fujii, and S. Ohtani, pp. 131-146, Am.  
439 Geophys. Union, Washington, D.C., 2000.

440 Richmond, A.D., E.C. Ridley, and R.G. Roble, A thermosphere/ionosphere general circula-  
441 tion model with coupled electrodynamics, *Geophys. Res. Lett.*, 19, 601-604, 1992.

442 Ridley, A.J., G. Crowley, and C. Freitas, An empirical model of the ionospheric electric  
443 potential, *Geophys. Res. Lett.*, 27, 3675-3678, 2000.

444 Ridley, A. J., Y. Deng, and G. Toth, The global ionosphere-thermosphere model, *J. Atmos.*  
445 *Sol-Terr. Phys.*, 68, 839, 2006.

446 Rishbeth, H., and I.C.F. Müller-Wodarg, Vertical circulation and thermospheric composition:  
447 a modelling study, *Ann Geophysicae*, 17, 794-805, 1999.

448 Roble, R.G., and E.C. Ridley, A thermosphere-ionosphere-mesosphere-electrodynamics gen-  
449 eral circulation model (time-GCM): equinox solar cycle minimum simulations (30-500 km),  
450 *Geophys. Res. Lett.*, 21, 417-420, 1994.

451 Roble, R.G., R.E. Dickinson, and E.C. Ridley, Global circulation and temperature structure  
452 of thermosphere with high-latitude plasma convection, *J. Geophys. Res.*, 87, 1599-1614, 1982.

453 Ruohoniemi, J.M., and R.A. Greenwald, Statistical patterns of high-latitude convection ob-  
454 tained from Goose Bay HF radar observations, *J. Geophys. Res.*, 101, 21,743-21,763, 1996.

455 Sharber, J.R., J.D. Winningham, R.A. Frahm, G. Crowley, A.J. Ridley, and R. Link, Empirical  
456 modeling of particle precipitation and the study of effects on the terrestrial thermosphere and  
457 ionosphere, *Phys. Chem. Earth C*, 25 489-493, 2000.

458 Smith, R.W., The global-scale effect of small-scale thermospheric disturbances, *J. Atmos.*  
459 *Solar-Terr. Phys.*, 62, 1623-1628, 2000.

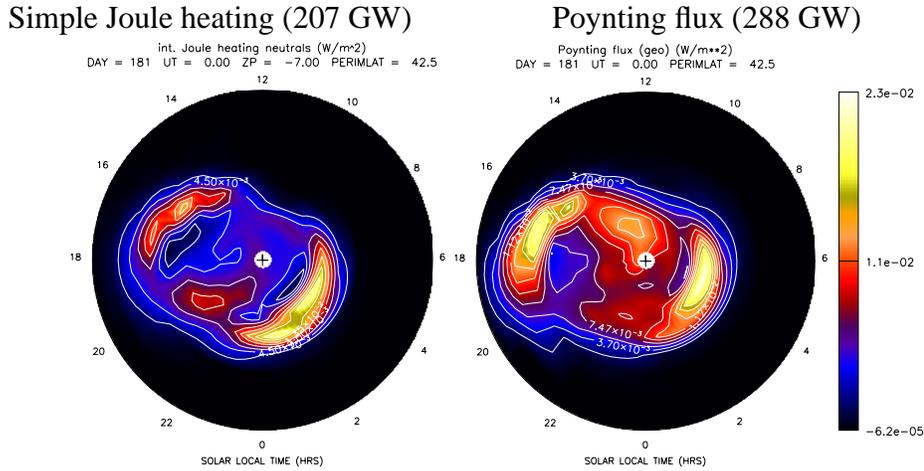
460 Thayer, J.P., J.F. Vickrey, R.A. Heelis, and J.B. Gary, Interpretation and modeling of the  
461 high-latitude electromagnetic energy flux, *J. Geophys. Res.*, 100, 19,715-19,728, 1995.

462 Volland, H., Magnetospheric electric fields and currents and their influence on large scale  
463 thermospheric circulation and composition, *J. Atmos. Solar-Terr. Phys.*, 41, 853-866, 1979.

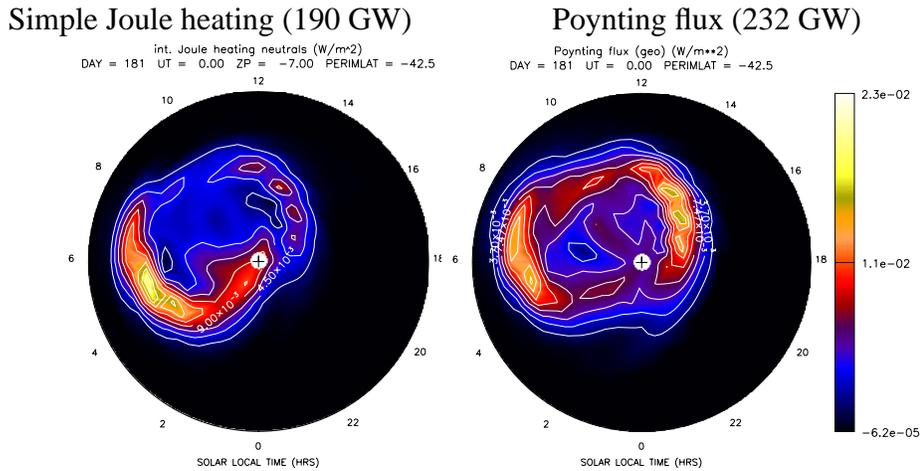
464 Weimer, D.R., An improved model of ionospheric electric potentials including substorm per-  
465 turbations and application to the Geospace Environment Modeling November 24, 1996, event,  
466 *J. Geophys. Res.*, 106, 407-416, 2001.

467 Weimer, D.R., Improved ionospheric electrodynamic models and application to calculating  
468 Joule heating rates, *J. Geophys. Res.*, 110, 5306+, 2005.

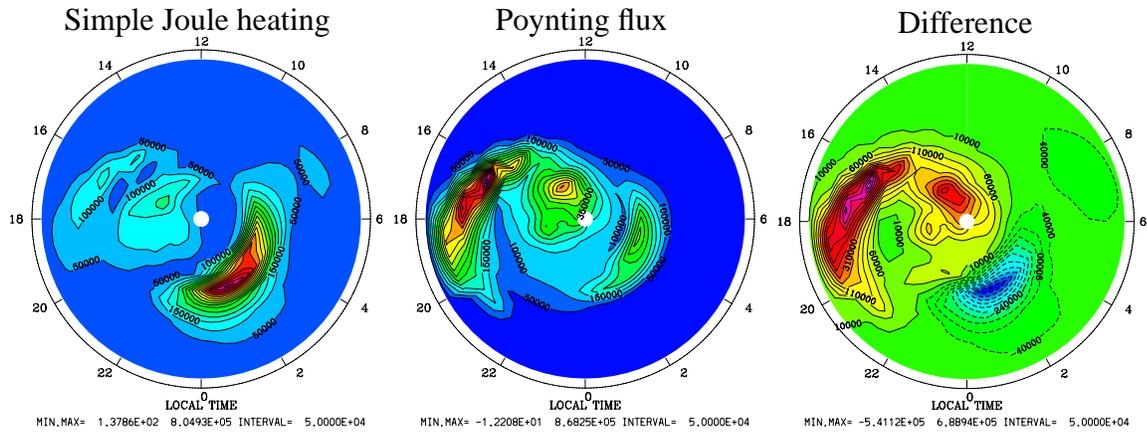
(A) Northern (Summer) hemisphere



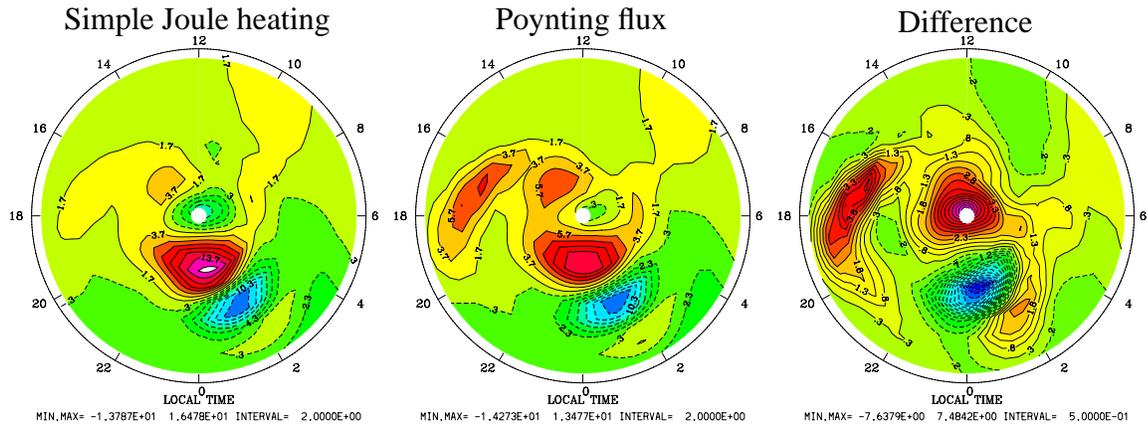
(B) Southern (winter) hemisphere



**Figure 1.** Total energy flux ( $W/m^2$ ) at the top of thermosphere from the magnetosphere for the (A) northern (summer) hemisphere and (B) southern (winter) hemisphere on DOY=181. The left column shows the altitude-integrated simple Joule heating and the right column shows the Poynting flux from the empirical model. The total energy is shown in brackets in the title. The outside ring is  $42.5^\circ$  geographic latitude for the northern hemisphere and  $-42.5^\circ$  for the southern hemisphere. All of the polar distributions in this paper are plotted in geographic coordinates.

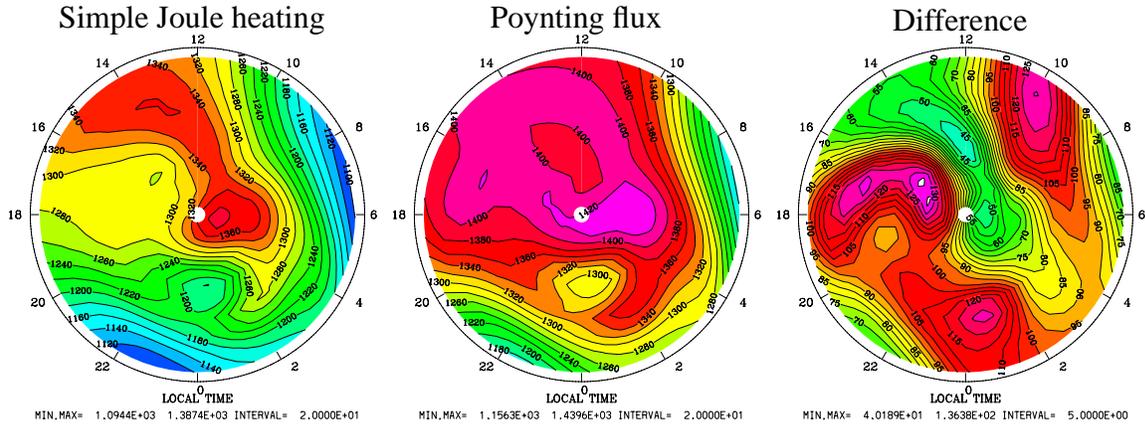


**Figure 2.** Heating per unit mass ( $erg/g/s [= 10^{-4}W/kg]$ ) at 400 km altitude in the northern (summer) hemisphere for (Left) the simple Joule heating case, (Middle) the Poynting flux case and (Right) the difference between these two cases. Note that the difference distribution has different scale than the heating distributions.

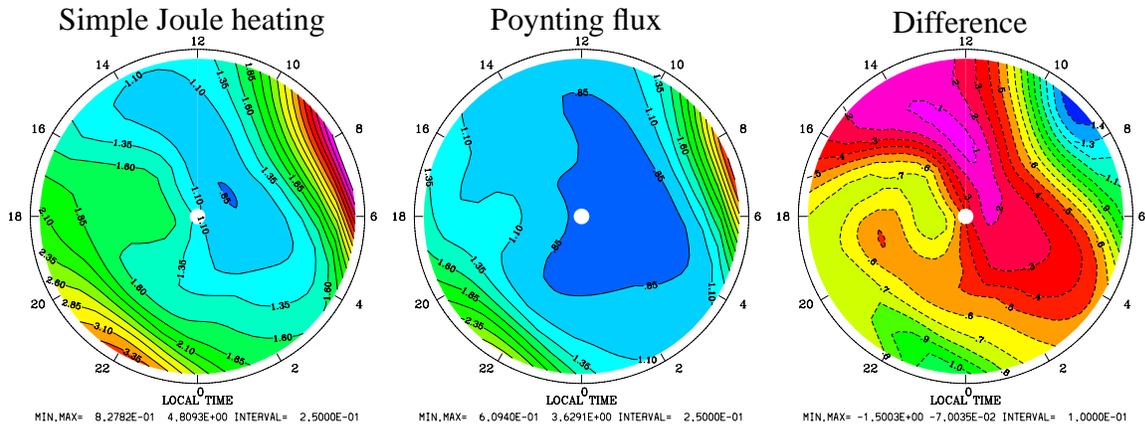


**Figure 3.** Same as Figure 2, but for vertical neutral wind ( $m/s$ ). Note that the scale for the difference velocity is amplified by a factor of 2.

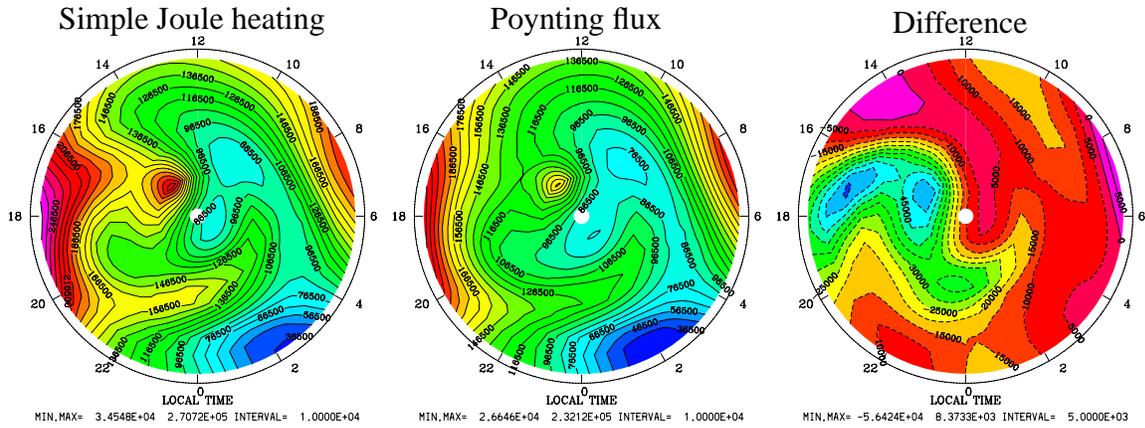
(A) neutral temperature (K)



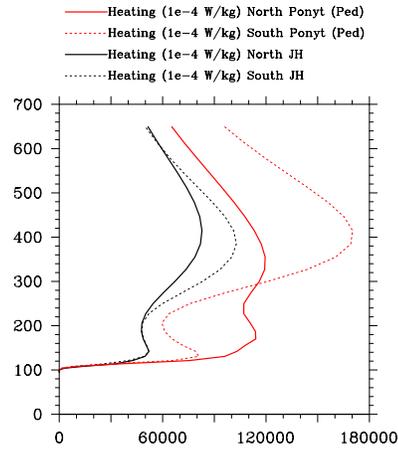
(B)  $O/N_2$  ratio



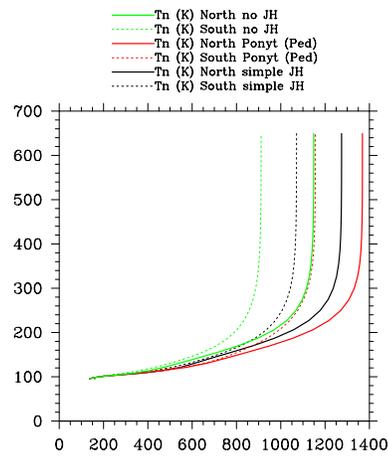
(C) Electron concentration ( $cm^{-3}$ )



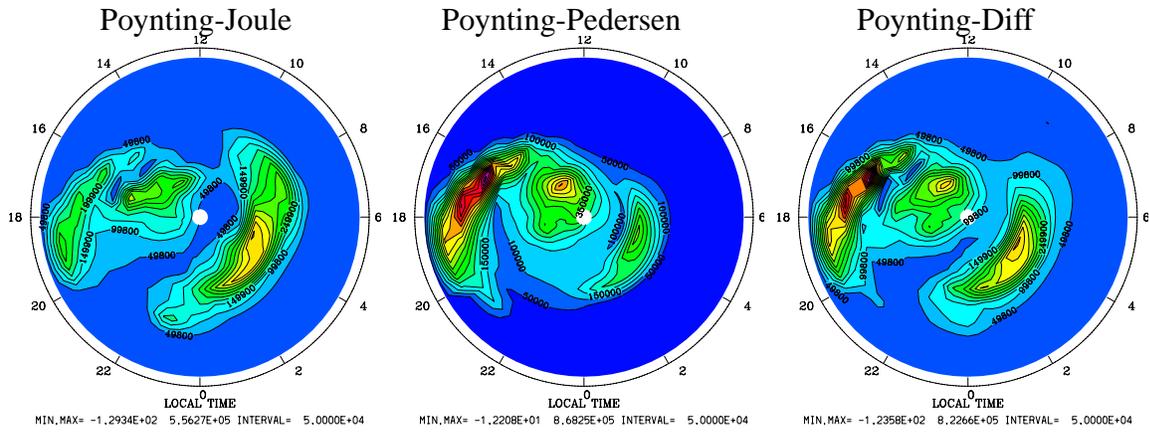
**Figure 4.** Same as Figure 2, but (A) for neutral temperature (K), (B) for composition ( $O/N_2$  ratio) and (C) for electron density ( $cm^{-3}$ ).



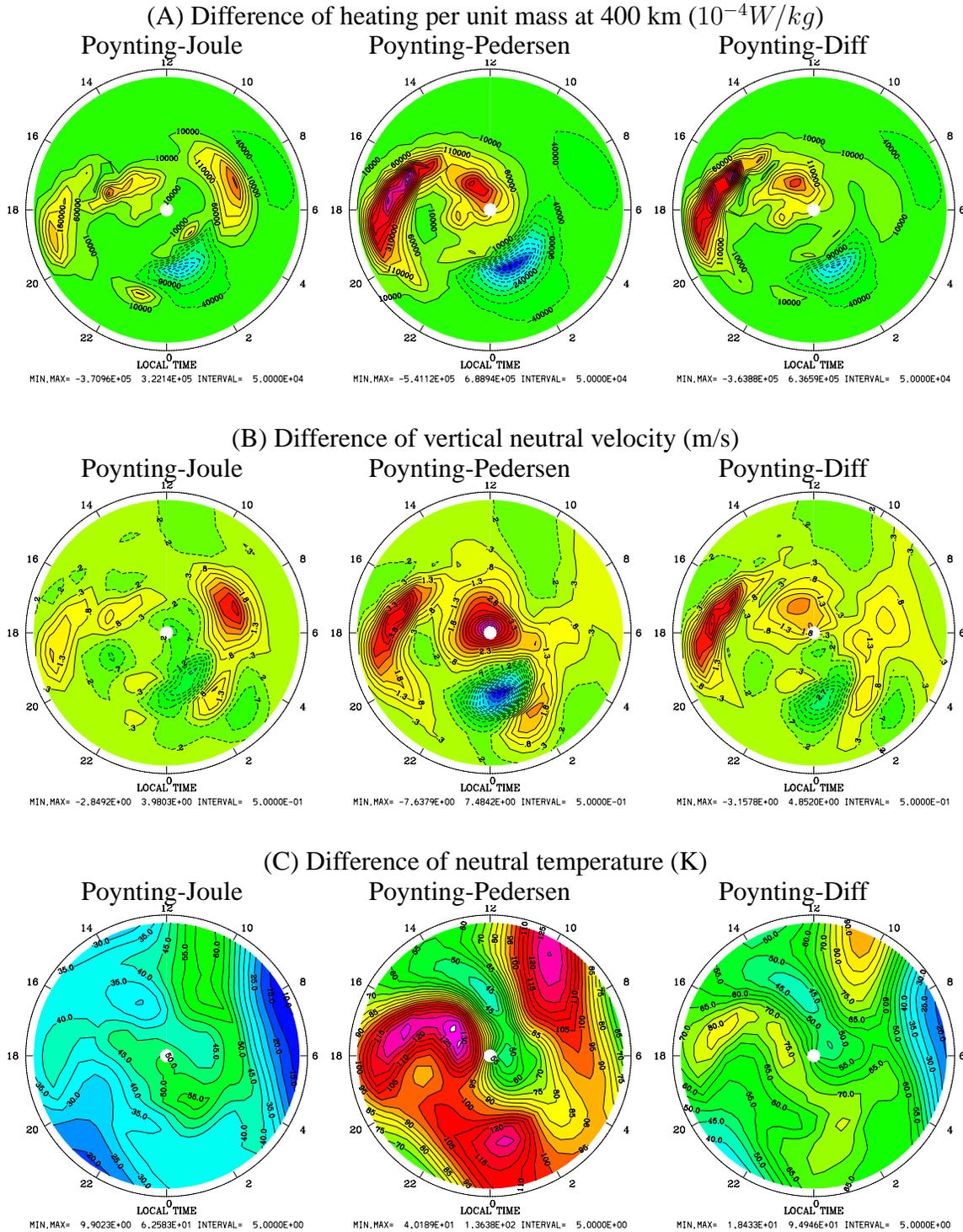
**Figure 5.** Altitude profile of the polar average (poleward  $40^\circ$  for the northern hemisphere and  $-40^\circ$  for the southern hemisphere) heating per unit mass ( $erg/g/s [= 10^{-4} W/kg]$ ) for the simple Joule heating case (black lines) and Poynting flux case (red lines). The solid lines represent the northern (summer) hemisphere and the dash lines represent the southern (winter) hemisphere.



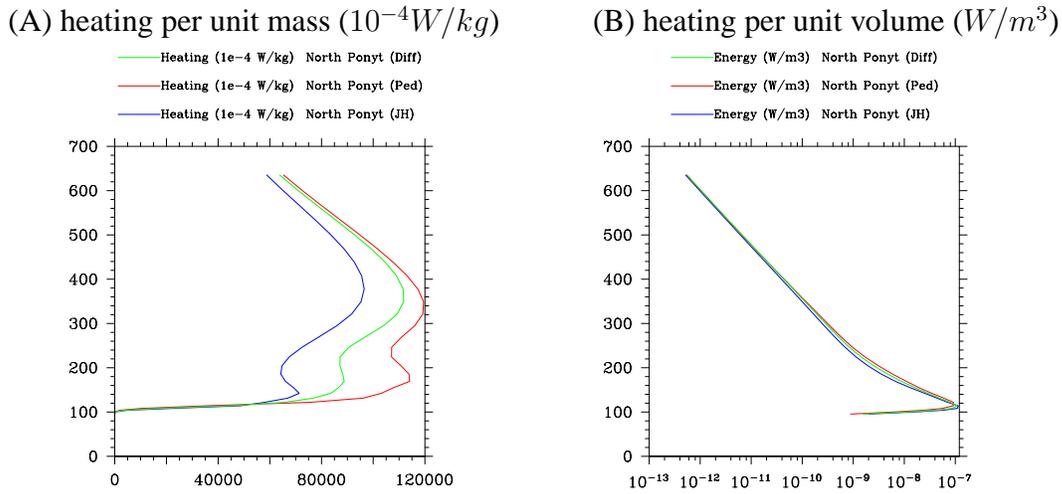
**Figure 6.** Altitude profile of the polar average (poleward  $40^\circ$  for the northern hemisphere and  $-40^\circ$  for the southern hemisphere) neutral temperature (K) for the case without Joule heating in the polar region (blue lines), the simple Joule heating case (black lines) and Poynting flux case (red lines). The solid lines represent the northern (summer) hemisphere and the dash lines represent the southern (winter) hemisphere.



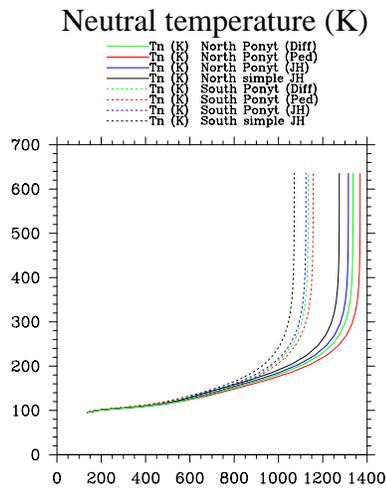
**Figure 7.** heating per unit mass ( $erg/g/s [= 10^{-4} W/kg]$ ) at 400 km altitude in the northern (summer) hemisphere for the (left) Poynting-Joule, (middle) Poynting-Pedersen and (right) Poynting-Diff cases.



**Figure 8.** The difference of (A) heating per unit mass ( $10^{-4}W/kg$ ), (B) vertical neutral velocity (m/s) and (C) neutral temperature (K) at 400 km altitude in the northern (summer) hemisphere when compared to the simple Joule heating case. The right column shows the Poynting-Joule case, the middle column shows the Poynting-Pedersen case and the right column shows the Poynting-Diff case.



**Figure 9.** Same as Figure 5, but blue lines for the Poynt (JH) case, red lines for the Poynt (Ped) case and the green lines for the Poynt (Diff) case.



**Figure 10.** Same as Figure 6, but black lines for the simple Joule heating case, blue lines for the Poynting-Joule case, red lines for the Poynting-Pedersen case and the green lines for the Poynting-Diff case.